

## **AP**<sup>®</sup> Physics B 2002 Free-Response Questions

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#### TABLE OF INFORMATION FOR 2002

CONSTANTS AND CONVERSION FACTORS		UNITS		PREFIXES			
1 unified atomic mass unit,	$1 \text{ u} = 1.66 \times 10^{-27} \text{ kg}$	Name	Symbol	Factor	<u>Prefix</u>	Symbol	
T diffred atomic mass diffe,	$= 931 \text{ MeV/}c^2$	meter	m	10 <sup>9</sup>	giga	G	
Proton mass,	$m_p = 1.67 \times 10^{-27} \text{ kg}$	kilogram	kg	10 <sup>6</sup>	mega	M	
Neutron mass,	$m_p = 1.67 \times 10^{-27} \text{ kg}$ $m_n = 1.67 \times 10^{-27} \text{ kg}$	second	s	10 <sup>3</sup>	kilo	k	
Electron mass,	$m_e = 9.11 \times 10^{-31} \text{ kg}$	ampere	A	$10^{-2}$	centi	c	
Magnitude of the electron charge,	$e = 1.60 \times 10^{-19} \mathrm{C}$	kelvin	K	$10^{-3}$	milli	m	
Avogadro's number,	$N_0 = 6.02 \times 10^{23} \mathrm{mol}^{-1}$	mole	mol	$10^{-6}$	micro	μ	
Universal gas constant,	$R = 8.31 \text{ J/(mol \cdot K)}$	hertz	Hz	$10^{-9}$	nano	n	
Boltzmann's constant,	$k_B = 1.38 \times 10^{-23} \text{J/K}$	newton	N	$10^{-12}$	pico	р	
Speed of light,	$c = 3.00 \times 10^8 \text{ m/s}$	pascal	Pa		1.		
Planck's constant,	$h = 6.63 \times 10^{-34} \text{J} \cdot \text{s}$ $= 4.14 \times 10^{-15} \text{eV} \cdot \text{s}$				F TRIGONOM OR COMMO		NCTIONS
		joule	J	θ	sin θ	$\cos \theta$	tan θ
	$hc = 1.99 \times 10^{-25} \text{J} \cdot \text{m}$	watt	W C				
	$= 1.24 \times 10^3  \text{eV} \cdot \text{nm}$	coulomb	V	0°	0	1	0
Vacuum permittivity,	$\epsilon_0 = 8.85 \times 10^{-12} \mathrm{C}^2 /\mathrm{N} \cdot \mathrm{m}^2$	volt		30°	1/2	$\sqrt{3}/2$	$\sqrt{3}/3$
Coulomb's law constant,	$k = 1/4\pi\epsilon_0 = 9.0 \times 10^9 \mathrm{N} \cdot \mathrm{m}^2/\mathrm{C}^2$	ohm	Ω H			•••	<b>V</b> = 1.0
Vacuum permeability,	$\mu_0 = 4\pi \times 10^{-7} (\mathrm{T \cdot m}) / \mathrm{A}$	henry		37°	3/5	4/5	3/4
Magnetic constant,	$k' = \mu_0 / 4\pi = 10^{-7} (T \cdot m) / A$	farad	F	45°	$\sqrt{2}/2$	$\sqrt{2}/2$	1
Universal gravitational constant,	$G = 6.67 \times 10^{-11} \text{ m}^3/\text{kg} \cdot \text{s}^2$	tesla	T	45	<b>V</b> 212	<b>V</b> 212	1
Acceleration due to gravity at the Earth's surface,	$g = 9.8 \mathrm{m/s^2}$	degree Celsius	°C	53°	4/5	3/5	4/3
1 atmosphere pressure,	1 atm = $1.0 \times 10^5 \text{ N/m}^2$	electron- volt	eV	60°	$\sqrt{3}/2$	1/2	$\sqrt{3}$
	$= 1.0 \times 10^5 \text{ Pa}$	VOIL	. ,		<b>V</b> 312	1/2	
1 electron volt,	$1 \text{ eV} = 1.60 \times 10^{-19} \text{ J}$			90°	1	0	∞
						I	1
		1		L			

The following conventions are used in this examination.

- I. Unless otherwise stated, the frame of reference of any problem is assumed to be inertial.
- II. The direction of any electric current is the direction of flow of positive charge (conventional current).
- III. For any isolated electric charge, the electric potential is defined as zero at an infinite distance from the charge.
- IV. For mechanics and thermodynamics equations, W represents the work done on a system.

#### ADVANCED PLACEMENT PHYSICS B EQUATIONS FOR 2002

#### **NEWTONIAN MECHANICS**

υ	=	$v_0$	+	at
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a = acceleration

$$x = x_0 + v_0 t + \frac{1}{2} a t^2$$

F = forcef = frequency

$$x = x_0 + v_0 t + \frac{1}{2} a t^2$$

h = height

$$v^2 = {v_0}^2 + 2a(x - x_0)$$

J = impulseK = kinetic energy

k = spring constant

$$\sum \mathbf{F} = \mathbf{F}_{net} = m\mathbf{a}$$

 $\ell = length$ m = mass

$$F_{fric} \le \mu N$$

N = normal force

$$a_c = \frac{v^2}{v^2}$$

P = power

$$a_c = \frac{v^2}{r}$$

p = momentumr = radius or distance

$$\tau = rF \sin \theta$$

 $\mathbf{r}$  = position vector

$$\tau = rF \sin \theta$$

T = periodt = time

 $\mathbf{p} = m\mathbf{v}$ 

U = potential energy

v = velocity or speed

 $\mathbf{J} = \mathbf{F}\Delta t = \Delta \mathbf{p}$ 

W = work done on a system

x = position

 $\mu$  = coefficient of friction

 $K = \frac{1}{2} m v^2$ 

 $\theta$  = angle

$$\tau = \text{torque}$$

$$\Delta U_g = mgh$$

$$W = \mathbf{F} \cdot \Delta \mathbf{r} = F \Delta r \cos \theta$$

$$P_{avg} = \frac{W}{\Delta t}$$

$$P = \mathbf{F} \cdot \mathbf{v} = F v \cos \theta$$

$$\mathbf{F}_s = -k\mathbf{x}$$

$$U_s = \frac{1}{2} kx^2$$

$$T_s = 2\pi \sqrt{\frac{m}{k}}$$

$$T_p = 2\pi \sqrt{\frac{\ell}{g}}$$

$$T = \frac{1}{f}$$

$$F_G = -\frac{Gm_1m_2}{r^2}$$

$$U_G = -\frac{Gm_1m_2}{r}$$

#### ELECTRICITY AND MAGNETISM

$$F = \frac{1}{4\pi\epsilon} \frac{q_1 q_2}{r^2}$$

A = area

$$F = \frac{1}{4\pi\epsilon_0} \frac{q_1 q_2}{r^2}$$

B = magnetic fieldC = capacitance

d = distance

$$\mathbf{E} = \frac{\mathbf{F}}{q}$$

E = electric field $\varepsilon = \text{emf}$ 

$$U_E = qV = \frac{1}{4\pi\epsilon_0} \frac{q_1 q_2}{r}$$

I = current $\ell$  = length

$$E_{avg} = -\frac{V}{d}$$

P = powerQ = charge

$$V = \frac{1}{4\pi\epsilon_0} \sum_{i} \frac{q_i}{r_i}$$

q = point chargeR = resistancer = distance

 $\rho$  = resistivity

 $\phi_m$  = magnetic flux

$$C = \frac{Q}{V}$$

t = time

$$C = \frac{\epsilon_0 A}{d}$$

U = potential (stored) energy V = electric potential or

$$d$$

$$U_c = \frac{1}{2}QV = \frac{1}{2}CV^2$$

potential difference v = velocity or speed

$$I_{avg} = \frac{\Delta Q}{\Delta t}$$

$$R = \frac{\rho \ell}{A}$$

$$K = \frac{1}{A}$$

$$V = IR$$

$$P = IV$$

$$C_p = \sum_i C_i$$

$$\frac{1}{C_s} = \sum_{i} \frac{1}{C_i}$$

$$R_{s} = \sum_{i} R_{i}$$

$$\frac{1}{R_p} = \sum_{i} \frac{1}{R_i}$$

$$F_B = qv B \sin \theta$$

$$F_B = BI\ell \sin \theta$$

$$B = \frac{\mu_0}{2\pi} \frac{I}{r}$$

$$\phi_m = \mathbf{B} \cdot \mathbf{A} = BA \cos \theta$$

$$\varepsilon_{avg} = -\frac{\Delta\phi_{m}}{\Delta t}$$

$$\varepsilon = B\ell v$$

#### FLUID MECHANICS AND THERMAL PHYSICS

$p = p_0 + \rho g h$	A = area
$F_{buoy} = \rho Vg$	c = specific heat or molar
, and the second	specific heat
$A_1 v_1 = A_2 v_2$	e = efficiency
$p + \rho g y + \frac{1}{2} \rho v^2 = \text{const.}$	F = force
$p + p_8 y + 2 p_0 = \text{const.}$	h = depth
$\Delta \ell = \alpha \ell_0 \Delta T$	$K_{avg}$ = average molecular
	kinetic energy
Q = mL	L = heat of transformation
$Q = mc\Delta T$	$\ell = length$
2	<i>M</i> = molecular mass
$p = \frac{F}{A}$	m = mass of sample
P = A	n = number of moles
pV = nRT	p = pressure
p, mei	Q = heat transferred to a system
$K_{avg} = \frac{3}{2} k_B T$	T = temperature
$\kappa_{avg} = \frac{1}{2} \kappa_B I$	U = internal energy
[2.P.T.	V = volume
$v_{rms} = \sqrt{\frac{3RT}{M}} = \sqrt{\frac{3k_BT}{\mu}}$	v = velocity or speed
$M = V M = V \mu$	$v_{rms}$ = root-mean-square
$W = -p\Delta V$	velocity
,, , , , , , , , , , , , , , , , , , , ,	W = work done on a system
$Q = nc\Delta T$	y = height
AU O I W	$\alpha$ = coefficient of linear
$\Delta U = Q + W$	expansion
$\Delta U = nc_V \Delta T$	$\mu$ = mass of molecule
==	$\rho = \text{density}$
W	

# lecular ergy rmation

$$\Delta U = Q + W$$
 expansion  
 $\Delta U = nc_V \Delta T$   $\mu = \text{mass of molecule}$   
 $\alpha = \text{density}$ 

$$e = \left| \frac{W}{Q_H} \right|$$

$$e_c = \frac{T_H - T_C}{T_H}$$

#### ATOMIC AND NUCLEAR PHYSICS

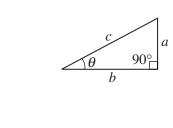
$$E = hf = pc$$
  $E = \text{energy}$   
 $K_{\text{max}} = hf - \phi$   $K = \text{kinetic energy}$   
 $\lambda = \frac{h}{p}$   $p = \text{momentum}$   
 $\lambda = \text{wavelength}$   
 $\Delta E = (\Delta m)c^2$   $\phi = \text{work function}$ 

#### WAVES AND OPTICS

$$v = f\lambda$$
  $d = \text{separation}$ 
 $n = \frac{c}{v}$   $length$ 
 $n_1 \sin \theta_1 = n_2 \sin \theta_2$   $length$ 
 $sin \theta_C = \frac{n_2}{n_1}$   $length$ 
 $sin \theta_C = \frac{n_2}{n_1}$   $length$ 
 $sin \theta_C = \frac{n_2}{n_1}$   $length$ 
 $length$ 

#### GEOMETRY AND TRIGONOMETRY

Rectangle	A = area
A = bh	C = circumference
Triangle	V = volume
$A = \frac{1}{2}bh$	S = surface area
$A = \frac{1}{2}bn$	b = base
Circle	h = height
$A = \pi r^2$	$\ell = length$
$C = 2\pi r$	w = width
Parallelepiped	r = radius
$V = \ell w h$	
Cylinder	
$V = \pi r^2 \ell$	
$S = 2\pi r\ell + 2\pi r^2$	
Sphere	
$V = \frac{4}{3} \pi r^3$	
$S = 4\pi r^2$	



Right Triangle  $a^2 + b^2 = c^2$ 

 $\sin\theta = \frac{a}{c}$ 

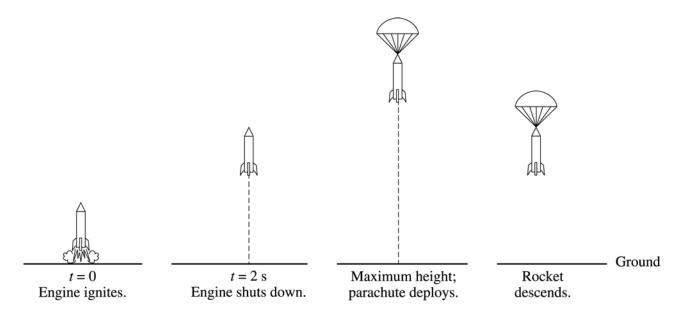
 $\cos \theta = \frac{b}{c}$ 

### PHYSICS B SECTION II

Time—90 minutes

7 Questions

**Directions:** Answer all seven questions, which are weighted according to the points indicated. The suggested time is about 15 minutes for answering each of questions 1-4, and about 10 minutes for answering each of questions 5-7. The parts within a question may not have equal weight. Show all your work in the pink booklet in the spaces provided after each part, NOT in this green insert.



Note: Figures not drawn to scale.

#### 1. (15 points)

A model rocket of mass 0.250 kg is launched vertically with an engine that is ignited at time t = 0, as shown above. The engine provides an impulse of  $20.0 \text{ N} \cdot \text{s}$  by firing for 2.0 s. Upon reaching its maximum height, the rocket deploys a parachute, and then descends vertically to the ground.

- (a) On the figures below, draw and label a free-body diagram for the rocket during each of the following intervals.
  - i. While the engine is firing
- ii. After the engine stops, but before the parachute is deployed
- iii. After the parachute is deployed

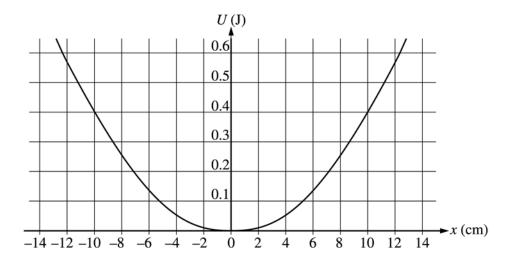






- (b) Determine the magnitude of the average acceleration of the rocket during the 2 s firing of the engine.
- (c) What maximum height will the rocket reach?
- (d) At what time after t = 0 will the maximum height be reached?

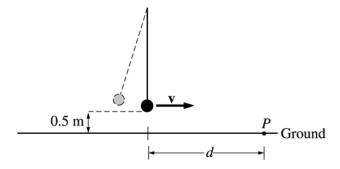
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#### 2. (15 points)

A 3.0 kg object subject to a restoring force F is undergoing simple harmonic motion with a small amplitude. The potential energy U of the object as a function of distance x from its equilibrium position is shown above. This particular object has a total energy E of 0.4 J.

- (a) What is the object's potential energy when its displacement is +4 cm from its equilibrium position?
- (b) What is the farthest the object moves along the x-axis in the positive direction? Explain your reasoning.
- (c) Determine the object's kinetic energy when its displacement is -7 cm.
- (d) What is the object's speed at x = 0?



Note: Figure not drawn to scale.

(e) Suppose the object undergoes this motion because it is the bob of a simple pendulum as shown above. If the object breaks loose from the string at the instant the pendulum reaches its lowest point and hits the ground at point *P* shown, what is the horizontal distance *d* that it travels?

#### 3. (15 points)

Two lightbulbs, one rated 30 W at 120 V and another rated 40 W at 120 V, are arranged in two different circuits.

- (a) The two bulbs are first connected in parallel to a 120 V source.
  - i. Determine the resistance of the bulb rated 30 W and the current in it when it is connected in this circuit.
  - ii. Determine the resistance of the bulb rated 40 W and the current in it when it is connected in this circuit.
- (b) The bulbs are now connected in series with each other and a 120 V source.
  - i. Determine the resistance of the bulb rated 30 W and the current in it when it is connected in this circuit.
  - ii. Determine the resistance of the bulb rated 40 W and the current in it when it is connected in this circuit.

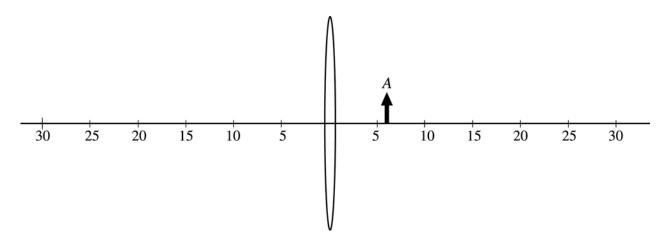
In the spaces below, number the bulbs in each situation described, in order of their brightness. $(1 = brightest, 4 = dimmest)$
30 W bulb in the parallel circuit
40 W bulb in the parallel circuit
30 W bulb in the series circuit
40 W bulb in the series circuit
Calculate the total power dissipated by the two bulbs in each of the following cases.
(

- i. The parallel circuit
- ii. The series circuit

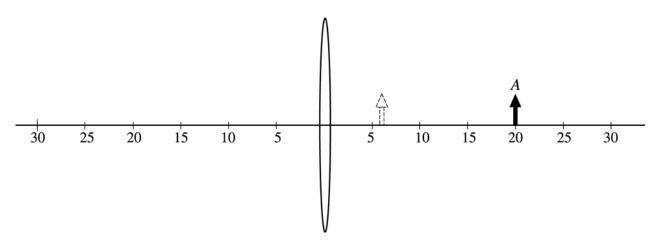
#### 4. (15 points)

A thin converging lens of focal length 10 cm is used as a simple magnifier to examine an object A that is held 6 cm from the lens.

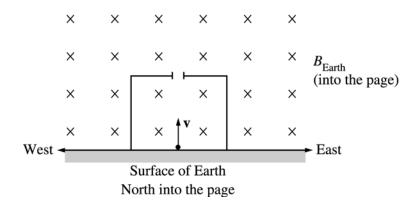
(a) On the figure below, draw a ray diagram showing the position and size of the image formed.



- (b) State whether the image is real or virtual. Explain your reasoning.
- (c) Calculate the distance of the image from the center of the lens.
- (d) Calculate the ratio of the image size to the object size.



(e) The object A is now moved to the right from x = 6 cm to a position of x = 20 cm, as shown above. Describe the image position, size, and orientation when the object is at x = 20 cm.



#### 5. (10 points)

A proton of mass  $m_p$  and charge e is in a box that contains an electric field E, and the box is located in Earth's magnetic field  $B_{\text{Earth}}$ . The proton moves with an initial velocity  $\mathbf{v}$  vertically upward from the surface of Earth. Assume gravity is negligible.

- (a) On the diagram above, indicate the direction of the electric field inside the box so that there is no change in the trajectory of the proton while it moves upward in the box. Explain your reasoning.
- (b) Determine the speed of the proton while in the box if it continues to move vertically upward. Express your answer in terms of the fields and the given quantities.

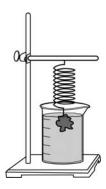
The proton now exits the box through the opening at the top.

- (c) On the figure on the previous page, sketch the path of the proton after it leaves the box.
- (d) Determine the magnitude of the acceleration a of the proton just after it leaves the box, in terms of the given quantities and fundamental constants.

#### 6. (10 points)

In the laboratory, you are given a cylindrical beaker containing a fluid and you are asked to determine the density  $\rho$  of the fluid. You are to use a spring of negligible mass and unknown spring constant k attached to a stand. An irregularly shaped object of known mass m and density D ( $D >> \rho$ ) hangs from the spring. You may also choose from among the following items to complete the task.

- A metric ruler
- A stopwatch
- String
- (a) Explain how you could experimentally determine the spring constant k.



- (b) The spring-object system is now arranged so that the object (but none of the spring) is immersed in the unknown fluid, as shown above. Describe any changes that are observed in the spring-object system and explain why they occur.
- (c) Explain how you could experimentally determine the density of the fluid.
- (d) Show explicitly, using equations, how you will use your measurements to calculate the fluid density  $\rho$ . Start by identifying any symbols you use in your equations.

Symbol	Physical quantity



#### 7. (10 points)

A photon of wavelength  $2.0 \times 10^{-11}$  m strikes a free electron of mass  $m_e$  that is initially at rest, as shown above left. After the collision, the photon is shifted in wavelength by an amount  $\Delta \lambda = 2h/m_e c$ , and reversed in direction, as shown above right.

- (a) Determine the energy in joules of the incident photon.
- (b) Determine the magnitude of the momentum of the incident photon.
- (c) Indicate below whether the photon wavelength is increased or decreased by the interaction.

Increased	Decreased
Explain your reasoning.	

(d) Determine the magnitude of the momentum acquired by the electron.

#### **END OF EXAMINATION**